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Conditional Source-term Estimation (CSE) and Conditional Moment Closure (CMC) in relation to piloted jet flames: a study of similarities and differences

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abstract

Direct side-by-side comparison of the Sandia flames is used to examine Conditional Moment Closure (CMC) and Conditional Source-term Estimation (CSE). The purpose of this research is to compare the efficacy of various modeling approaches under similar situations and computational frameworks. We evaluate the accuracy of CMC and CSE predictions against extensive experimental data. In the instance of Sandia flame D, the turbulent flow and mixing fields predicted by CMC and CSE are identical close to the nozzle exit, in accordance with the actual observations, but they diverge farther downstream. Good agreement exists between the experimental results obtained downstream of the nozzle for lean mixtures and the conditional mass fractions calculated using CMC and CSE for the principal species. There are several axial sites for fuel-rich mixtures where the conditional mass proportion of methane is underestimated while the conditional mass fraction of water is overestimated. The main features of the experimental profiles are recapitulated by the CMC and CSE conditional mass fractions of the minor species and conditional temperature. However, Sandia flame E is drastically different. It has been determined that RANS, along with boundary conditions established in CMC and certain assumptions made in the chemical tables in CSE, are to blame for the observed differences. Both CMC and CSE Favre-averaged profiles are similar. Time spent running each model in the computer is compared, with CSE coming out on top. Further, some of the benefits and drawbacks of each combustion model are discussed. Results are proven to be of equivalent quality between CMC and CSE when the same numerical techniques, mesh, and boundary conditions are used.

Keywords: CMC Inferno of the CSE SANDIA D type FLAME OF SANDIA E Combustion Turbulence

Introduction

Closure for the mean chemical source term using conditional averaged quantities is provided by Conditional Moment Closure (CMC) [1,2] and Conditional Source-term Estimation (CSE) [3,4]. The underlying assumption of these models is that changes in species mass fractions and temperature (or enthalpy) may be linked to changes in one or more scalars that can be used as conditioning variables. In most standard formulations, only one conditioning variable is taken into account, such as the mixture fraction in non-premixed combustion. The thin flame assumption is unnecessary in the CMC or CSE derivation, expanding its

application. The conditional response rates are closed to first order in flames that are distant from extinction or igniting [4], since the fluctuations around the conditional averages are minor and can be ignored. In this way, specific the incorporation of chemistry can be done at little computational cost. As an added bonus, the conditional averages exhibit substantially less spatial variability than their unconditional counterparts. Because of this, conditional averages may be computed using a spatial mesh that is coarser than the grid used to solve unconditional averages.

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E advancements, on the other hand, are more recent, build on CMC's capabilities while avoiding the closure of the extra terms included in the CMC transport equations. The conditional averages may be derived by inverting an integral equation, as shown in the first CSE article [3], which uses DNS data for an a priori test. While flamelet decomposition was used in the first iterations of integral inversion [24,25], a regularization approach with tabular precise chemistry is now used. Similar to CMC, CSE was first implemented for non-premixed instances and is continually evolving [24,25,27-31]. Recent years have seen advancements in our understanding of premixed combustion [26,32,33], multi-stream configurations [34,35], and partially-premixed flames [36-38]. In the latter two cases, CSE closes the mean reaction rates without the need for closure of extra and difficult terms by using the utilization of doubly conditionally averaged quantities. Key CSE elements for high performance are precise inversion using a regularization approach [39] and a chemistry table that is realistic of the fuel and the task at hand [30].

As can be seen, CMC and CSE have certain things in common, and each has advantages and disadvantages that may become apparent depending on the context. Both methods have progressed to the point where they can be compared side by side for the same turbulent flame inside the same Computational Fluids Dynamics (CFD) framework, and evaluated for their forecast accuracy, computational time, and potential.

The purpose of this analysis is to compare and contrast the various modeling approaches under identical settings and computational frameworks. We employ the same CFD numerical techniques, mesh, and boundary conditions for both sets of simulations to reduce inconsistencies. In order to provide a fair comparison between CMC and CSE, only RANS simulations are taken into account.

Since the two models are founded on the same fundamental idea, it is crucial to identify and address the factors contributing to the differences in their forecasts. Both conditional mass balance and conditional species equilibria (CMC and CSE) rely on the direct retrieval of the conditional mass fractions of species through the solution of transport equations or integral inversion, respectively. Numerical approximations and inaccuracies are introduced during the integral inversion procedure. No direct comparison with CMC has yet been done to evaluate the magnitude of this inaccuracy. Because of this, it is essential to evaluate whether or not the conditional profiles acquired by CSE through this inversion procedure are equivalent to those derived using the transport equations in CMC. The study presented here is the first to compare and contrast the two models head-to-head. In order to do this, we need well-

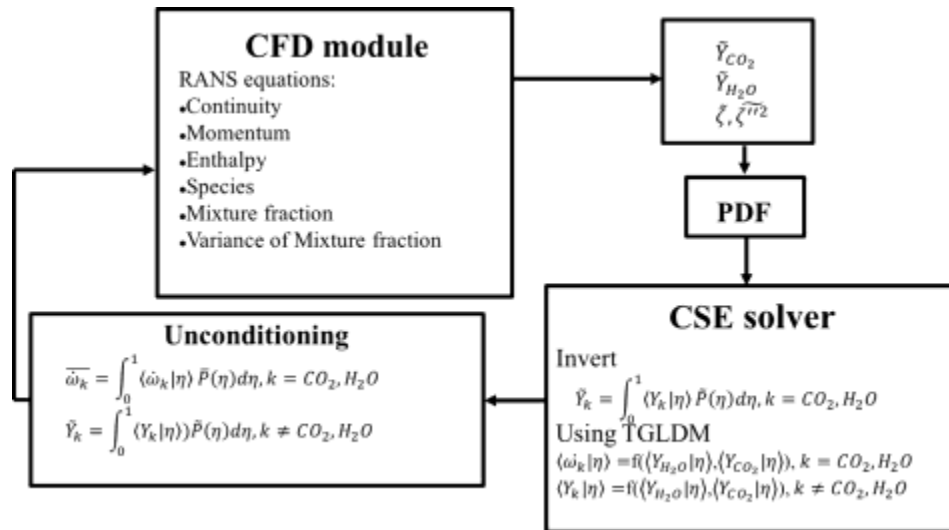
characterized examples of turbulent flames that have not been premixed. Detailed experimental data on the mean axial velocities, temperatures, Favre-averaged mass fractions, mean mixture fractions, and mixture fraction root mean squares suggest that the Sandia piloted jet flames are a promising contender.

(rms), and some conditional species concentrations at different locations [40].

Many turbulent combustion models in RANS and LES have been used to successfully simulate the Sandia flames. These models include a Lagrangian flamelet model [41], a steady flamelet formulation [42], a flamelet model including a progress variable [43], and various Probability Density Function (PDF) approaches [44-50]. As an additional point of reference, the Sandia flames have been used in a number of CMC and CSE research. Good agreement is found for the conditional mass fractions of the principal species and temperature for lean mixtures in RANS when using radially-averaged first order CMC incorporating radiation [7]. Inaccuracies in the chemical kinetics and non-negligible conditional fluctuations in fuel-rich areas explain the discrepancies reported between predictions and experimental evidence for fuel-rich mixes. Kronenburg and Kostka [23] provide a pretabulated dual conditioning approach that takes into account the impact of conditional fluctuations on conditional response rates. Since the primary species in the Sandia flame D do not significantly shift, the disagreement between our study and the findings previously reported by Roomina and Bilger [7] must arise from differences in chemical kinetics in the fuel-rich zone. While Brizuela and Roudsari [51] do compare their results to experimental data in conditional space, they do so in a restricted way. Predictions of species mass fractions are demonstrated to be enhanced by using second order CMC [52] and a second order Lagrangian CMC approach [53]. When utilizing second order CMC, however, we do not see any increase in extinction. Better spatial and temporal resolution of turbulent mixing in LES is demonstrated to allow for first order CMC to offer additional improvement compared to previous RANS predictions [54]. The LES-CMC grid sensitivity study [55] confirms this as well. Two different formulations have been used to simulate the Sandia flame D in the context of CSE. First using CSE in LES with a two-step chemical mechanism, Steiner and Bushe [56] found that their predictions were generally in line with the available experimental data. Later, a more refined CSE formulation is investigated, complete with tabulated chemistry; the resulting temperature and species concentration values are shown to be in excellent agreement with the experimental results [28]. No published CSE findings on the Sandia E and F flames have been found, as far as the authors are aware.

The current study's implementations of CMC and CSE are detailed below. The major goal is to directly contrast the predictions made by the various formulations. Furthermore, experimental data are provided as a reference point

Fig. 1. CSE code structure.



The combustion models CSE and CMC are available in OpenFOAM 2.3 CFD code [62]. When comparing CMC with CSE simulations, you'll find no differences in the boundary conditions, turbulence model, numerical scheme, mesh, or chemical process. In Section 4 we offer further details on the turbulence model, boundary conditions, mesh, and chemical process used in the numerical scheme. Since the formulation of the combustion model accounts for all differences in the predictions, this research provides a rare chance to directly compare the two models. Figures 1 and 2 show a schematic of the CMC and CSE programs' integration with the CFD solver.

The RANS-CMC technique used in this investigation calls for two different computational meshes, one for the RANS and one for the CMC. Given that conditional means exhibit far more variation across longer time periods than unconditional means, this is understandable. It is necessary to convert the information about the flow and mixing field from the coarser RANS-CFD resolution to the finer CMC resolution. By averaging over a large volume of data, we can calculate the conditional velocity, turbulent diffusivity, and unconditional scalar dissipation rate [63]. Previous LES-CMC implementations have discovered that mass weighted and PDF weighted averages are both appropriate, with only minor changes in the fi-

Experimental conditions

Since extensive experimental data is available, the methane/air non-premixed piloted Sandia flames

examined by Barlow and Frank [40] are chosen for this investigation. A 7.2 mm primary fuel jet and an 18.2 mm pilot are at the heart of the Sandia flames, which are located in a wind tunnel with a 0.9 m/s coflow of air. With a stoichiometric mixture fraction of 0.351, the primary fuel jet consists of 25% methane (CH₄) and 75% air by volume. At an equivalency ratio of 0.77, the pilot is a lean combination of ethyne (C₂H₂), hydrogen (H₂), air, carbon dioxide (CO₂), and ni- trogen (N₂). The primary jet of the Sandia flame D has a bulk velocity of 49.6 m/s (2 m/s), which corresponds to a Reynolds number of 22,400; the pilot's velocity is 11.4 m/s (0.5 m/s), which is the subject of the current investigation. An even more impressive quantity of local extinctions have been attributed to the Sandia flame E, which has a Reynolds number of 33,600.

investigation, as well.

Measurements of mass fraction of species, mixture fraction, temperature, and velocity at different axial positions have been obtained experimentally. Additional profiles of the mass fractions of species under various conditions are also accessible. Raman-Rayleigh-LIF measurements were used to get temperature, species, and mixture fraction information from experiments. Nitrogen (N₂), water vapor (H₂O), carbon dioxide (CO₂), hydrogen (H₂), carbon monoxide (CO), and hydroxide (OH) all have experimental uncertainties (OH)

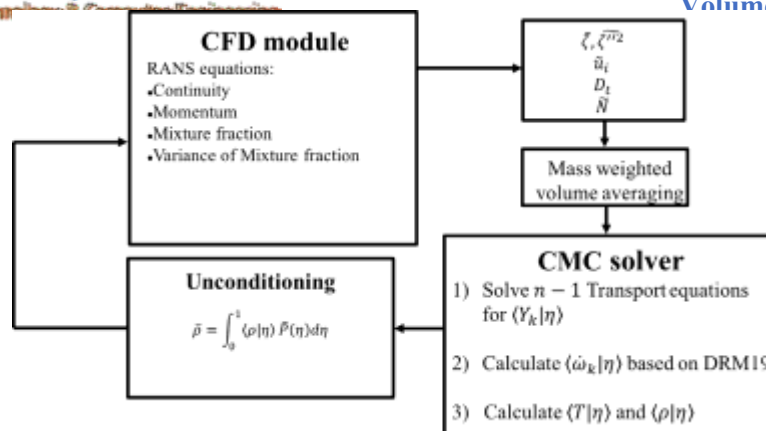


Fig. 2. CMC code structure.

Computational details

OpenFoam 2.3 [62] is a finite volume programme that uses the CSE and CMC models under the low Ma number assumption. Standard OpenFoam release combustion solvers use a PIMPLE pressure correction technique to solve the velocity field. In simulation, the time step may be changed. You may expect a maximum Courant number of 0.3.

CSE uses an integral inversion to calculate conditional averages, while CMC uses the solution of transport equations. Therefore, CMC and CSE need separate numerical methods. In order to solve problems involving finite differences, the CMC code [15,63] was developed. First and second order accurate total variation diminishing (TVD) schemes [64] are used to discretize the convective transport in Eqs. (1) and (2). Mixture fraction and physical space diffusion terms are discretized using a second-order accurate central difference technique. When the size of the system that needs to be solved concurrently is reduced, the computational burden is also reduced, and this is achieved via the use of full operator splitting. The system of ODEs for both the stiff and non-stiff portion of Eqs. (1) and (2) have been integrated using the solver VODPK [65]. (2). Adding transport equations for mixture percent and its variance, the present CSE algorithm is an expansion of the reactingFOAM combustion model. Both CMC and CSE use OpenFOAM's in-built numerical techniques to discretize these transport equations. As part of the inversion procedure, LU decomposition is used to get the solution to Equation (9).

In the current investigation, the computational domain is a small-angle wedge ($=5^\circ$) with a radius of 21D and a height of 100D, where D is the fuel intake diameter equal to 7.2 mm. A two-dimensional object is constructed from a single

cell in the direction of the arrow.

simulation. The nozzle areas are represented by a non-uniform grid in which the cell density is greater. The present mesh, consisting of 51,000 cells, has been proved to yield grid independent results after a succession of ever finer meshes were examined.

For the turbulent flow field, this study makes use of the k model [66]. The C1 constant is adjusted, as is customary in the k model, such that it agrees with the velocity estimates from experiments. Using a sensitivity analysis, we found that $C1 = 1.52$ provides the greatest fit to the data from the experiments. CMC and CSE simulations of methane/air combustion with 19 species and 84 reactions are accompanied by detailed kinetics utilizing the DRM19 mechanism [67]. Boundary conditions for velocities, temperatures, mixture fractions, turbulent kinetic energies, and Both the kinetic energy k and the dissipation rate of k are chosen to correspond with the range of obtainable experimental circumstances. For the pilot flow, the species mass fraction of CO₂ and H₂O are both adjusted to their equilibrium compositional values of 0.109 and 0.10006 at the boundary conditions, respectively [51].

Except for pressure, all other fields are constrained by an OpenFOAM zeroGradient boundary condition at the outlet. The outlet pressure boundary condition is set to 0.993 atm [40] while the jet, pilot, and coflow inlet pressure boundary conditions are all set to zeroGradient. Using the Sandia data set and an integral length scale of 1.4 mm, [68] the velocities, turbulent kinetic energies, and turbulent dissipation rates at the jet, pilot, and coflow inlets are determined. For the velocities k and, the intake profiles are discretized along the 30 cells of the pilot

and the jet. The possible values of the mixture fraction are discretized into

There are more data points clustered close to the stoichiometric mixture fraction than in any of the other 60 bins. There was very little variation in the predictions while doing simulations with a larger number of bins (90). In this way, we can say that the simulations do not rely on the degree of resolution in the space of mixture fractions. The conditional species mass fractions in CMC are based on a burning flamelet profile at the intake nodes. Mixed boundary conditions for CMC (burning in pilot, inert everywhere else) are not conceivable because of the small number of cells in the radial direction. When using a delta function mixture fraction PDF with the coflow, pilot, and fuel mass fractions of 0, 0.27, and 1, respectively, the flamelet profiles are defined in a way that preserves the right unconditional boundary values.

Setting the conditional mass fraction of CO₂ and H₂O profiles to generate high reaction rates from the TGLDM tables is the starting point for the CSE calculations. When the concentrations of YCO₂ and

YH₂O are not high enough to sustain combustion, the startup procedure is stopped. After this is done, the inversion yields the values for (YCO₂) and YH₂O.

Based on prior CSE research into non-premixed jet flames [27,34,35], 19 ensembles are defined as axial slices of the computational domain, making up a 19x1 CSE grid for the CSE simulations. It has been shown that CSE ensembles are not uniformly distributed, with a larger concentration towards the nozzle exit, where substantial changes to the mixture fraction are anticipated. In contrast, a 25x5 CMC grid is used in the CMC simulations. Thus, in the axial direction, the two simulations have the same spatial resolution, but in the radial direction, the CSE simulations assume the conditional averages stay constant. When comparing the CSE findings to the experimental data, a coarser CMC grid was tried and was shown to provide bigger disparities. Since it is well-known that the accuracy of CMC decreases when the number of cells is decreased, it is not practical to employ a coarser CMC grid in this case. *Sandia flame D*

could not be manufactured as fine as the CMC grid. Increasing the resolution of the CFD mesh and hence the number of reactive cells in the ensembles is required for this. In comparison, CMC may use a grid with the same precision as CFD. Still, the CMC transport equations can't be solved without taking into account the large number of CMC cells that reside in the coflowing air. Considering the lack of fuel and chemical processes, CSE excludes these cells from the inversion process. As a consequence, it is not anticipated nor essential that the CMC and CSE grids be equal in order to get comparable quality results. As shown in Fig. 3, the CSE ensembles and CMC grid are depicted in a schematic form.

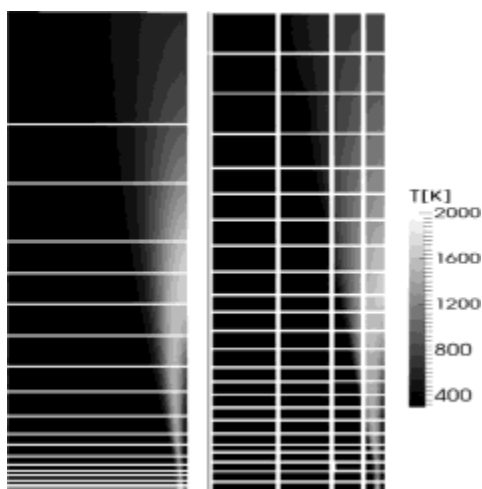


Fig. 3. Temperature contours with a schematic of the CSE ensembles (left) and CMC grid (right) superimposed.

presently existing circumstances. Unlike the CMC grid, the CSE grid must have a sufficient number of reacting cells for the inversion process, hence it

2. Results

The findings of the simulations of the Sandia flames are broken down into four categories for examination. It begins with a comprehensive breakdown of the Flame D simulation findings. The available experimental data at six axial points is first compared to the Favre-averaged velocity, mixture percent, and its root mean square (rms) generated from the CSE and CMC simulations. The conditional temperature, conditional mass fractions of CO₂, H₂O, CH₄, H₂, and OH, and experimental profiles at the same six axial positions are then compared. Although experimental data exists for a wider range of species, only a representative sample was included in this analysis. We may draw the same conclusions about other flames. Following this is a comparison of the Favre-averaged mass fractions and temperatures. Next, the Flame E findings are shown, with special attention paid to the area just next to the nozzle, where the CMC and CSE values diverge. For reasons that will be detailed below, neither model, in its present

configuration, was able to provide satisfactory findings for Sandia flame F. Finally, the computational cost of CSE and CMC are compared and contrasted, and the benefits and drawbacks of each method are discussed.

The 5.1.1 Field of Turbulent Flow

As shown in Fig. 4, the axial velocity derived from the CMC and CSE simulations agrees well with the actual data at six axial locations. The agreement between CMC, CSE, and the experimental data is excellent, with all values falling within 3 m/s of each other extremely near to the nozzle at $y/D = 3$. Further downstream at $y/D = 15$, the velocities predicted by CMC and CSE for radial locations between $r/D = 1$ and $r/D = 2$ are somewhat overpredicted compared to the observed profile. The centerline velocities generated from both the CMC and CSE simulations are around 16% greater than the value measured empirically at $y/D = 30$. The CMC and CSE estimated velocities off-axis accord well with the experiments. The first three axial points show a remarkable degree of agreement between the two numerical profiles.

distinct from one another. Greater discrepancies in velocity between the CMC and CSE models are shown farther downstream, at $y/D = 45$ and $y/D = 60$. Specifically, the centerline experimental velocity is overestimated by around 20% when CSE is applied at $y/D = 45$.

CMC's estimate for the centerline velocity is around 12% greater than the value derived through experiments. At $y/D = 60$, a similar pattern is observed: the center-line velocity calculated using CSE is 3 m/s higher than the actual data, but the velocity obtained using CMC is only around 2 m/s higher. Since the identical numbers for velocity, k , and are applied to both CMC and CSE, the discrepancies in the anticipated velocity profiles cannot be explained by changes in the simulations' boundary conditions. Instead, as demonstrated in Section 5.1.5, the divergences in the velocity field may be traced back to discrepancies in the temperature profiles produced by CMC and CSE. Any change in the temperature profiles will cause a change in the jet's spreading rate due to changes in

density, k , and. In spite of these minor deviations, the present velocity estimates agree with those of earlier numerical studies for the identical flame [7,55,69]. At this point, it is safe to say that both simulations produce a turbulent flow-field that is consistent with experimental results.

5.1.2 Field of turbulent mixing

The conditional species mass fraction is determined using the mixture fraction probability density function (PDF) in CMC and CSE. So, it's crucial that both CSE and CMC provide accurate predictions of the mean mixture fraction and its rms. In Figs. 5 and 6, we compare the mean mixture percent and its rms field from the CMC and CSE simulations to the experimental results at the same six axial sites.

Figure 5 displays the results for the values of y/D equal to 3, 15, and 30.

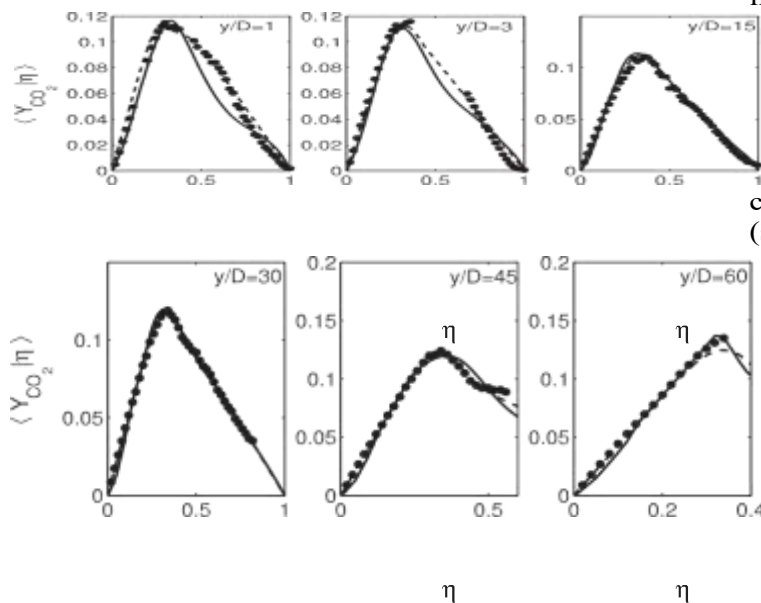
CMC and CSE projected mixture fraction profiles are consistent with experimental results. At $y/D = 45$, farther downstream, more striking variations emerge. Here, CSE's profile shape more closely matches experimental results, but CMC's peak profile fraction prediction is more accurate. The CMC findings reveal a greater overprediction of the mixture fraction profile compared to the CSE predictions between radial sites $r/D = 2$ and $r/D = 5$. Within 10%, the CSE predictions and the experimental profile correspond well at the final axial site ($y/D = 60$). The CMC values are likewise in excellent agreement with the experimental profile here, although they overpredict the mixture percent at radial positions between $r/D = 2.5$ and $r/D = 7$.

Several variants in the combination frac-

differences in tion rms between the two groups of numerical simulations. rms profiles from CMC and CSE are similar to one another close to the center.

correspond very closely throughout the whole axis. The experimental root-mean-square (rms) values between $r/D = 1$ and $y/D = 3$ are overpredicted by both CMC and CSE.0.5

Fig. 7. CSE (solid lines) and CMC (dashed lines) conditional CO_2 mass fraction profiles



compared to the experimental data [40] (symbols) at different axial locations.

should be exactly the same since they have the same principles in common. However, due to the fact that the conditional averages are generated using different methods—matrix inversion for CSE and transport equations for CMC—each model involves its own set of assumptions, modeling, and numerical mistakes. For this reason, it's possible to see deviations from the projected conditional mass fractions. The CO₂ and H₂O conditional mass fractions computed by CMC and CSE are first compared to the available experimental data [40] in Figs. 7 and 8.

The CSE simulations rely heavily on the conditional mass fractions of CO₂ and H₂O, which are retrieved together with the conditional mass fractions of the other species and the conditional mass temperature from the TGLDM tables, making accurate predictions of these quantities vital. As can be observed in Fig. 7, CSE does a calculations of YCO₂ using CSE, with the exception of the case when the value of YCO₂ is larger than what is seen experimentally (0.7). Mistakes in the predicted mixture fraction rms profiles, which would have an effect on the PDF,

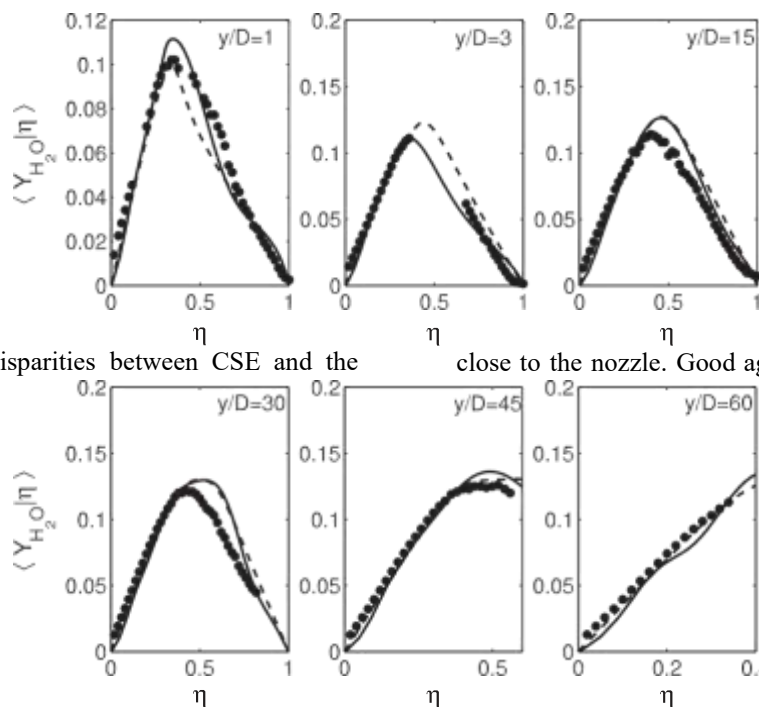
decent job of predicting the conditional mass fraction of CO₂ at $y/D = 1$ and $y/D = 3$, as compared to the experimental profiles.

Very excellent agreement with the trials is shown between $\eta = 0$ and $\eta = 0.5$ in these spots. Under-predictions of about 25% are seen for values between 0.5 and 0.77.

Fig. 8. CSE (solid lines) and CMC (dashed lines) conditional H₂O mass fraction profiles compared to the experimental data [40] (symbols) at different axial locations.

accurately by the inversion process employed in CSE without the usage of a submodel.

Figure 8 shows that similar patterns may be seen for the conditional mass fraction of H₂O derived from CSE as it is



may be to blame for the disparities between CSE and the

close to the nozzle. Good agreement is shown at $y/D = 1$ and

experimental results at these sites. At $y/D = 1$, the CSE and experimental numbers differ by around 2% from the CMC predictions, which reveal a peak in the conditional CO₂ mass fractions. While CMC and CSE profiles agree within 11% for lean mixes, CMC does a better job of capturing the conditional profiles for $\eta > 0.5$, with an underprediction of just 5% compared to 33% when using CSE at $\eta = 0.6$ and $y/D = 1$. CSE and the experimental data have agreed extremely well over the last $y/D = 3$, with the largest discrepancy being about 2% at $y/D = 15$ for $\eta = 0.31$. These are areas of very low population density, where

Both CMC and CSE have their own unique characteristics. Therefore, the CMC and CSE predictions are quite near to each other at places far from the nozzle where the boundary conditions do not affect the expected conditional averages. This convergence is encouraging since the conditional averages are determined by two unique approaches. This also shows that the conditional averages can be reproduced

$y/D = 3$, but the peak of YH₂O is underestimated by around 10% at $y/D = 1$. With respect to lean mixes, the CMC findings match well with the CSE and experimental data at the same sites, to within around 10%. However, the H₂O conditional mass fractions determined from CMC are almost 24% lower than the experimental values for rich mixes ($\eta = 0.36$). It is possible that the inconsistencies in the YH₂O profiles at $y/D = 1$ and $y/D = 3$ compared to the predictions of (YCO₂) are attributable to the choice of boundary conditions in CMC at the pilot boundary. At axial coordinates $y/D = 5$ and outward, Roomina and Bilger [7] detail the adiabatic equilibrium compositions of all reactive scalars except nitric oxides (NO). It is claimed that this approximation has little effect on downstream places. The

The present study's CMC findings corroborate this finding. When extrapolated to downstream regions, the CSE and CMC profiles are quite similar to one another, with a discrepancy of just 0.01 between them and the experimental data for 0.35.

Comparatively, the conditional mass fraction of H₂O is more than the experimental value for rich mixes with 0.37 0.77. The study of Roomina and Bilger [7] at $y/D = 30$ utilizing a wide range of chemical processes, including GRI 2.11[70], shows a similar pattern, with (YCO₂) for rich mixes being appropriately predicted but (YH₂O) being overestimated. For all axial sites beyond $y/D = 3$, CMC and CSE agree, proving that the inversion method used in CSE produces the same conditional profiles as CMC.

Figure 9 shows that the CSE and CMC conditional mass fraction of CH₄ closely tracks the experimental profile at $y/D = 1$ and $y/D = 3$. Since the primary combustion products, (YCO₂) and (YH₂O), are well predicted (Figs. 7 and 8), the strong agreement revealed by CSE and CMC at these sites for fuel lean mixes is to be anticipated. The increased conditional mass fractions of H₂O found for fuel rich mixes in both sets of simulations are reflected in the CMC and CSE profiles that are near to and below the actual values for 0.5 at $y/D = 15$ and y/D

Computational Time Comparison

Currently, the CSE code has not been optimized in any way. For matrix inversions of a comparable size, recent research by Hong and Bushe [71] has shown that switching from the LU decomposition matrix solver utilized in the present work to the LSQR solver may result in a 19–55% reduction in computing time. On the other hand, the present CMC code is the result of a more protracted period of development by groups at Ghent University [15,16] and the University of Cambridge [12,17,18].

It has been determined that the CSE submodel alone accounts for over 85% of the computational time in RANS-CSE. Matrix inversion, extraction of conditional species and reaction rate data from TGLDM tables, and computation of unconditional species and reaction rates are all part of the CSE submodel. 15% of the CPU time is spent calculating transport equations for pressure, velocity, mixture fraction, mixture fraction variance, and mass fraction of CO₂ and H₂O. The CSE combustion model takes around 7.6 seconds for a single timestep when run on a cluster of Intel Xeon E5-2680v3 processors operating at 2.5 GHz utilizing a single processing core. The CMC subroutines account for almost all of the CPU time in the RANS/CMC computations. Single timesteps for CMC on the same cluster operating on five cores take around 3.6 seconds, with a total computational resource need of about 18 CPU seconds. In the current computational cost, the CPU time required to build the TGLDM tables is not accounted for. CSE looks to be quicker than CMC for the present calculations based on CPU time, without any optimization and including the time required to generate the chemical tables. Furthermore, based on the time needed to determine the conditional average of a single species, a rough estimate of the computing time necessary for CSE without optimization or tabular chemistry is provided. As used in CSE, this is the

= 30, as shown in Fig. 8. As is shown in the CMC findings of Roomina and Bilger [7], the conditional reaction rates of CH₄ are overpredicted for fuel rich combinations in most flame areas.

FIGURE 10: The H₂ mass fraction under various conditions. H₂ has a higher disparity between the conditional mass fractions predicted by CSE and CMC compared to CO₂, H₂O, and CH₄. Both the CSE and the CMC profiles shrink down at $y/D = 1$, whereas the experimental profile remains quite wide. Both CMC and CSE overestimate the peak conditional mass fractions of H₂ at this point, however CSE does a somewhat better job of forecasting where this peak will be in the context of the total mixture fraction. The H₂ values for rich mixture fractions are underestimated by CSE, although the CMC and CSE agree well for lean mixture fractions at downstream $y/D = 3$. CMC and CSE forecasts at $y/D = 15$ accord rather well with the experimental profile. Farther

sum of the times it takes to do the inversion and to solve the unconditional species transport equation. In the current investigation, a single conditional average requires around 0.32 seconds of CPU time to calculate. On the other hand, a single CMC transport equation can be solved in around 0.12 CPU seconds. Therefore, CSE is about 2.6 times slower than CMC in calculating the conditional averages in the absence of optimization and chemistry tabulation. In CSE, without tabular chemistry, this data allows for a ballpark approximation of the calculation time required. A CSE model without tabular chemistry would need about 21.8 CPU seconds, which is 20% greater than CMC assuming the only computational time difference between the two programs was the computation of the conditional averages.

Comparison of the CMC and CSE methodologies: 5.2.

Given the identical numerical setup, sections 5.1.1-5.1.5 showed that CMC and CSE could generate predictions that were in excellent agreement with each other. The advantages and disadvantages of each method used in the present research are discussed below.

CMC calls for far more intricate boundary conditions to be put up correctly than CSE does. The mixture percent, its variance, and the mass fraction of YCO₂ and YH₂O are all necessary boundary conditions in CSE, and they may be easily computed from experimental data. Comparatively, CMC necessitates boundary conditions for mixture fraction, its variance, conditional temperature, and conditional mass fraction of all species. As a result, these conditional profiles have to be estimated rather than acquired directly from the experimental data.

As a result of how the CMC is now implemented, incorporating new chemical schemes is simpler. Substituting one chemical mechanism for another has no effect on the CMC recipe. In addition, CMC can simulate intricate fuel composition without any

kind of special treatment. The TGLDM method is used for tabulation of chemical data in the current CSE model. Thus

Conclusions

Both CMC and CSE are studied here by comparing the Sandia flames side by side. To reduce the likelihood of inconsistencies between the two models, the identical CFD numerical techniques, mesh, and boundary conditions are utilized for both sets of simulations. The results of CMC and CSE are compared to extensive experimental data.

Near the nozzle exit, the turbulent flow and mixing fields in the CMC and CSE simulations are consistent with experimental results. Away from the centerline and farther downstream, there are noticeable inconsistencies between the CMC and CSE profiles, as well as with the experimental data. Near the nozzle, the mixture fraction rms exhibits the same trends and overall shape for both CMC and CSE models. In the downstream region, the rms values of the mixture fractions are less in the CMC findings compared to the CSE and the experimental data. The anticipated temperature profiles from CMC and CSE are different, which accounts for the discrepancy in forecasts.

For lean mixtures, the conditional mass fractions predicted by CMC and CSE for the principal species are in excellent agreement with actual data downstream of the nozzle, with the CMC and CSE findings frequently being indistinguishable. The conditional mass fractions of CH₄ and H₂O in fuel-rich mixes are underpredicted and overestimated, respectively, at particular axial sites. The main features of the experimental profiles are recapitulated by the CMC and CSE conditional mass fractions of the minor species and conditional temperature. Larger discrepancies between CMC and CSE are seen for the minor species, and they are due to the various approaches used to determine the chemical source-term (calculated during the simulation in CMC and retrieved from pre-tabulated chemistry tables in CSE). Large gradients at the boundary in the TGLDM tables lead to bigger deviations in the CSE conditional mass fractions of H₂ and OH in fuel-rich mixes. Differences between CMC and CSE at the nozzle exit are explained by the use of CMC boundary conditions.

In both CMC and CSE simulations, the same general tendencies are reproduced from the Favre-averaged profiles, and equivalent quality simulation results are achieved. It has been predicted by CMC and CSE that the flame would spread outward from the nozzle. The volume and broad patterns of the downstream are accurately reproduced by CMC and CSE. profiles of the main temperature and species groups. For the minor species derived via CMC and CSE, the disparities between the experimental data and Favre-averaged profiles are higher than for the conditional profiles.

The jet velocity, turbulence-chemistry interactions, and local extinction are all more prominent in Sandia flame E, making the choice of combustion model

more crucial. The CSE simulations mimic the higher level of local extinction, which is observable in lower temperatures and large species mass fractions, but to an unrealistic degree. There is a disconnect between this tendency and how CMC is currently implemented. Only with LES is it possible to account for the velocity fluctuations and implement more advanced boundary conditions, both of which are necessary for achieving optimal results with CMC. As a corollary, conditional scalar dissipation modeling is crucial. Both models failed to successfully simulate Sandia flame F at the present conditions.

A look at the computing time needed for each combustion model reveals that CMC takes higher computational resources for the present flame. Further, some of the benefits and drawbacks of each combustion model are discussed. The CSE method is easier to use when it comes to defining the boundary conditions, while the CMC method is more convenient when it comes to setting up the mesh needed for the conditional averages.

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